

Please write clearly, in block capitals.

Centre number

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Candidate number

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Candidate signature

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# A-level MATHEMATICS

## Paper 3

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Exam Date

Morning

Time allowed: 2 hours

### Materials

For this paper you must have:

- The AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

### Instructions

- Use black ink or black ball-point pen. Pencil should be used for drawing.
- Answer **all** questions.
- You must answer each question in the space provided for that question. If you require extra space, use an AQA supplementary answer book; do **not** use the space provided for a different question.
- Do not write outside the box around each page.
- Show all necessary working; otherwise marks for method may be lost.
- Do all rough work in this book. Cross through any work that you do not want to be marked.

### Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 100.

### Advice

Unless stated otherwise, you may quote formulae, without proof, from the booklet. You do not necessarily need to use all the space provided.

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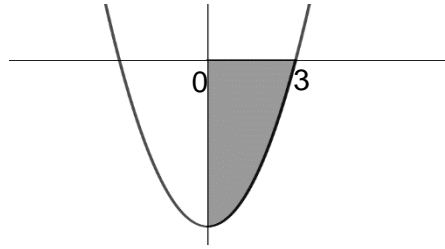
**Section A**


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Answer **all** questions in the spaces provided.

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- 1** The graph of  $y = x^2 - 9$  is shown below.



Find the area of the shaded region.  
Circle your answer.

[1 mark]

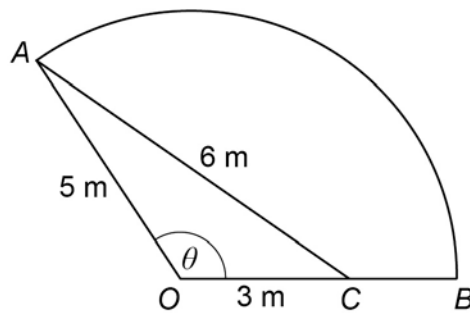
-18

-6

6

18

- 2** A wooden frame is to be made to support some garden decking. The frame is to be in the shape of a sector of a circle. The sector  $OAB$  is shown in the diagram, with a wooden plank  $AC$  added to the frame for strength.  $OA$  makes an angle of  $\theta$  with  $OB$ .



- 2 (a)** Show that the exact value of  $\sin \theta$  is  $\frac{4\sqrt{14}}{15}$

[3 marks]

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**2 (b)** Write down the value of  $\theta$  in radians to 3 significant figures.

**[1 mark]**

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**2 (c)** Find the area of the garden that will be covered by the decking.

**[2 marks]**

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**3 (b) (iii)** How many days does it take for the weed to cover half of the surface of the pond?

**[2 marks]**

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**3 (c)** State one limitation of the model.

**[1 mark]**

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**3 (d)** Suggest one refinement that could be made to improve the model.

**[1 mark]**

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- 5 (a)** Find the first three terms, in ascending powers of  $x$ , in the binomial expansion of  $(1 + 6x)^{\frac{1}{3}}$

**[2 marks]**

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- 5 (b)** Use the result from part **(a)** to obtain an approximation to  $\sqrt[3]{1.18}$  giving your answer to 4 decimal places.

**[2 marks]**

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- 5 (c)** Explain why substituting  $x = \frac{1}{2}$  into your answer to part **(a)** does not lead to a valid approximation for  $\sqrt[3]{4}$ .

**[1 mark]**

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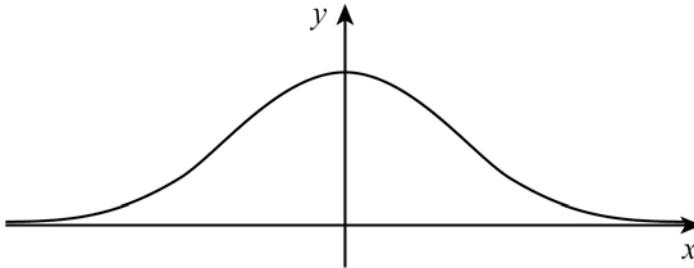
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- 7 The diagram shows part of the graph of  $y = e^{-x^2}$



The graph is formed from two convex sections, where the gradient is increasing, and one concave section, where the gradient is decreasing.

- 7 (a) Find the values of  $x$  for which the graph is concave.

[4 marks]

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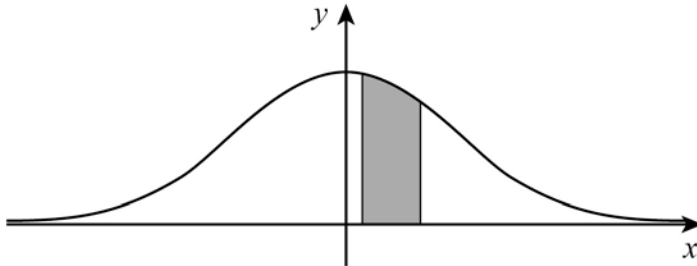
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- 7 (b) The finite region bounded by the  $x$ -axis and the lines  $x = 0.1$  and  $x = 0.5$  is shaded.



Use the trapezium rule, with 4 strips, to find an estimate for  $\int_{0.1}^{0.5} e^{-x^2} dx$

Give your estimate to four decimal places.

[3 marks]

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Question 7 continues on the next page

- 7 (c)** Explain with reference to your answer in part **(a)**, why the answer you found in part **(b)** is an underestimate.

**[2 marks]**

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**7 (d)** By considering the area of a rectangle, and using your answer to part **(b)**, prove that the shaded area is 0.4 correct to 1 decimal place.

**[3 marks]**

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**END OF SECTION A  
TURN OVER FOR SECTION B**

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**Section B**

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Answer **all** questions in the spaces provided.

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- 8** Edna wishes to investigate the energy intake from eating out at restaurants for the households in her village.

She wants a sample of 100 households.

She has a list of all 2065 households in the village.

Ralph suggests this selection method.

“Number the households 0000 to 2064. Obtain 100 different four-digit random numbers between 0000 and 2064 and select the corresponding households for inclusion in the investigation.”

- 8 (a)** What is the population for this investigation?

Circle your answer.

**[1 mark]**

Edna and Ralph	The 2065 households in the village	The energy intake for the village from eating out	The 100 households selected
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- 8 (b)** What is the sampling method suggested by Ralph?

Circle your answer.

**[1 mark]**

Opportunity	Random number	Continuous random variable	Simple random
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**9** A survey has found that, of the 2400 households in Growmore, 1680 eat home-grown fruit and vegetables.

**9 (a)** Using the binomial distribution, find the probability that, out of a random sample of 25 households in Growmore, exactly 22 eat home-grown fruit and vegetables.

**[2 marks]**

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**9 (b)** Give a reason why you would **not** expect your calculation in part **(a)** to be valid for the 25 households in Gifford Terrace, a residential road in Growmore.

**[1 mark]**

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10 Some information from the Large Data Set is given in Figures 1 and 2 below.

Figure 1

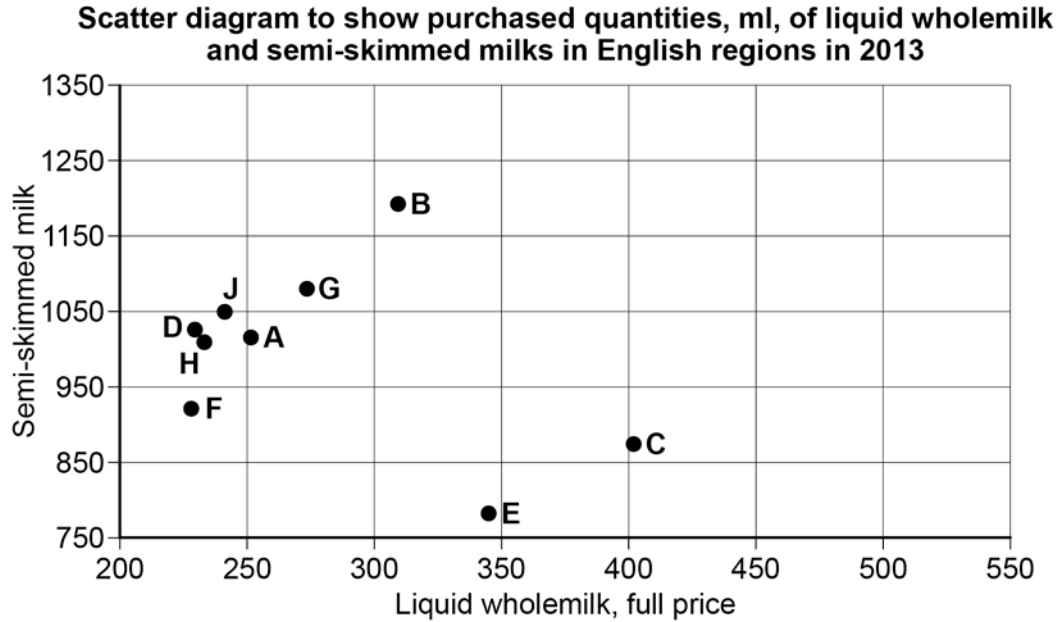
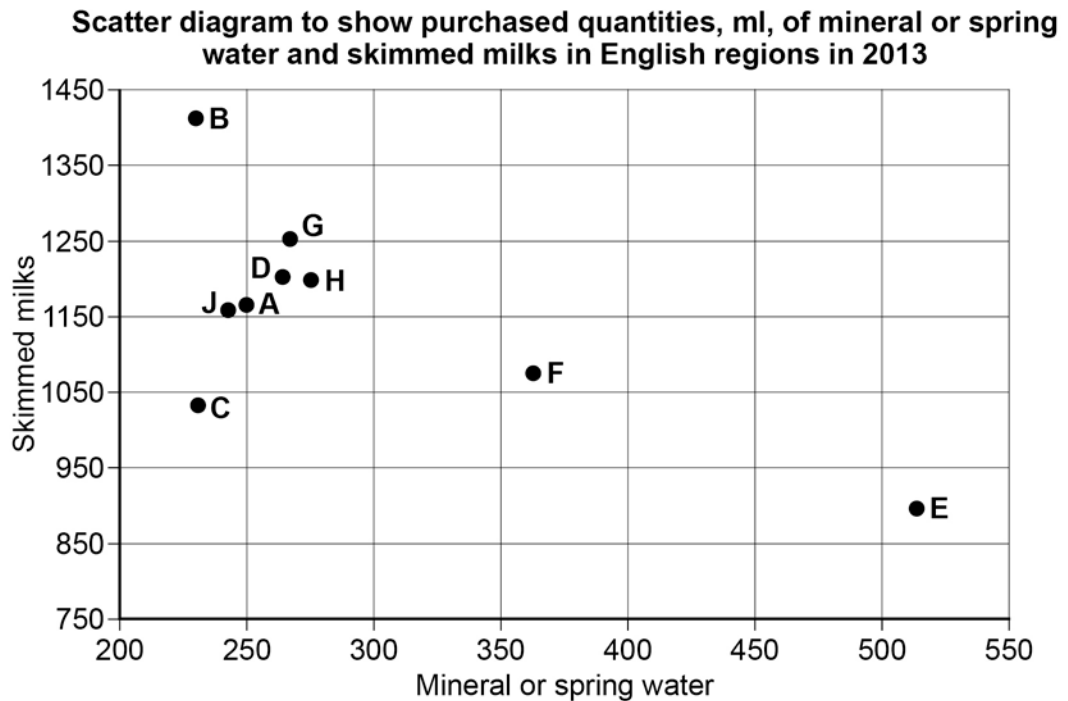


Figure 2





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**10 (a)** Give a reason why the recorded vertical data values are higher for each region in Figure 2 than in Figure 1 **[1 mark]**

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**10 (b) (i)** Describe the correlation between 'Semi-skimmed milk' and 'Liquid wholemilk, full price'. **[2 marks]**

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**10 (b) (ii)** Bilal claims that Figure 2 indicates that when people drink more mineral or spring water they tend to drink less skimmed milk.  
Comment on Bilal's claim. **[2 marks]**

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**Question 10 continues on the next page**

**10 (c)** Suggest, with a reason, which region is indicated by the letter E. Use your knowledge of the Large Data Set to support your answer.

**[2 marks]**

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- 11** Terence owns a local shop. His shop has three checkouts, at least one of which is always staffed.

A regular customer observed that the probability distribution for  $N$ , the number of checkouts that are staffed at any given time during the spring, is

$$P(N = n) = \begin{cases} \frac{3}{4} \left(\frac{1}{4}\right)^{n-1} & \text{for } n = 1, 2 \\ k & \text{for } n = 3 \end{cases}$$

- 11 (a)** Find the value of  $k$ .

**[1 mark]**

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- 11 (b)** Find the probability that a customer, visiting Terence's shop during the spring, will find at least 2 checkouts staffed.

**[2 marks]**

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**12 (b)** State **two** assumptions, regarding illness during the Christmas holidays, that are necessary for the distribution you have used in part **(a)** to be valid.

For **each** assumption, comment, in context, on whether it is likely to be correct.

**[4 marks]**

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**Turn over for the next question**

- 13** In the South West region of England, 100 households were randomly selected and, for each household, the weekly expenditure, £ $X$ , per person on food and drink was recorded.

The maximum amount recorded was £40.48 and the minimum amount recorded was £22.00

The results are summarised below, where  $\bar{x}$  denotes the sample mean.

$$\sum x = 3046.14 \qquad \sum (x - \bar{x})^2 = 1746.29$$

- 13 (a) (i)** Find the mean of  $X$

Find the standard deviation of  $X$

**[2 marks]**

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- 13 (a) (ii)** Using your results from part **(a)(i)** and other information given, explain why the normal distribution can be used to model  $X$ .

**[2 marks]**

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- 13 (a) (iii)** Find the probability that a household in the South West spends less than £25.00 on food and drink per person per week.

[1 mark]

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- 13 (b)** For households in the North West of England, the weekly expenditure, £ $Y$ , per person on food and drink can be modelled by a normal distribution with mean £29.55

It is known that  $P(Y < 30) = 0.55$

Find the standard deviation of  $Y$ , giving your answer to one decimal place.

[3 marks]

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Turn over for the next question





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- 14 (b)** The 2013 survey revealed that the mean expenditure per adult, per week on alcohol was 324p.

The mean expenditure per adult per week on alcohol for 2009 was 307p.

A test was carried out on the following hypotheses relating to mean expenditure per adult per week on alcohol in 2013.

$$H_0 : \mu = 307$$

$$H_1 : \mu \neq 307$$

This test resulted in the null hypothesis,  $H_0$ , being rejected.

State, with a reason, whether the test result supports the following statements:

- 14 (b) (i)** the mean UK expenditure on alcohol per adult per week increased by 17p from 2009 to 2013;

**[2 marks]**

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- 14 (b) (ii)** the mean UK consumption of alcohol per adult per week changed from 2009 to 2013.

**[2 marks]**

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